

$$\underline{v}_1 \quad \underline{v}_2 \quad \underline{v}_3$$

$$\begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} \quad \begin{pmatrix} -1 \\ 2 \\ 1 \end{pmatrix} \quad \begin{pmatrix} 0 \\ 2 \\ 1 \end{pmatrix}$$

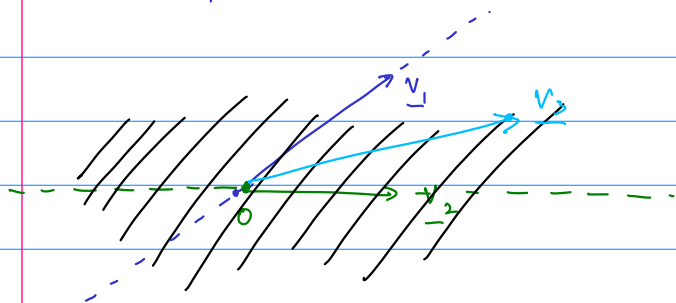
$$\alpha_1 \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} -1 \\ 2 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 0 \\ 2 \\ 1 \end{pmatrix}$$

+ Set of all linear combinations (L).

* Does $\begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} \in L$?

Can $\begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$ be written as a linear comb of $\underline{v}_1, \underline{v}_2, \underline{v}_3$?

$$\alpha \underline{v}_1 + \beta \underline{v}_1 = (\alpha + \beta) \underline{v}_1$$



DOT PRODUCTS

$$1. \quad \underline{v}_1 = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} \quad \underline{v}_2 = \begin{pmatrix} -1 \\ 2 \\ 1 \end{pmatrix}$$

$$\underline{v}_1 \cdot \underline{v}_2 = 1(-1) + 2(2) + 1(1) = 4.$$

2. If $\underline{v} \cdot \underline{w} = 0$, we say $\underline{v}$ and $\underline{w}$ are orthogonal.

$$3. \quad (\text{Length of } \underline{v})^2 = \underline{v} \cdot \underline{v}.$$